

Look at the frequency tables.  
How could you represent the data?

1

kids	freq
0	1
1	3
2	7
3	3
4	1

2

kids	freq
0	3
1	3
2	3
3	3
4	3

3

kids	freq
0	5
1	3
2	3
3	2
4	2

4

kids	freq
0	1
1	2
2	3
3	4
4	5

5

kids	freq
0	5
1	2
2	1
3	2
4	5

How would the representations look  
for each frequency table?

which chart goes with which data set?

1

kids	freq
0	1
1	3
2	7
3	3
4	1

2

kids	freq
0	3
1	3
2	3
3	3
4	3

3

kids	freq
0	5
1	3
2	3
3	2
4	2

4

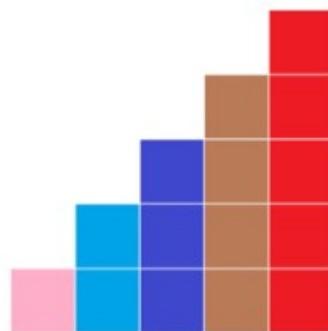
kids	freq
0	1
1	2
2	3
3	4
4	5

5

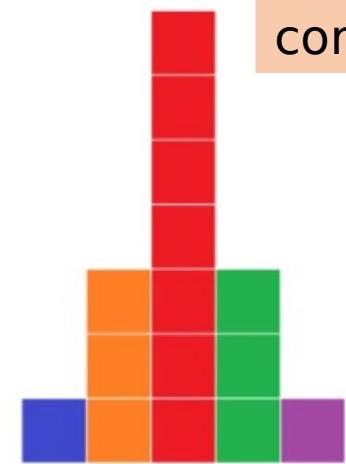
kids	freq
0	5
1	2
2	1
3	2
4	5



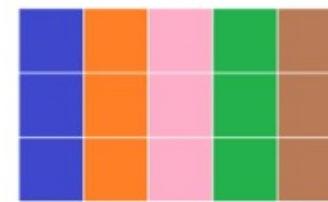
a



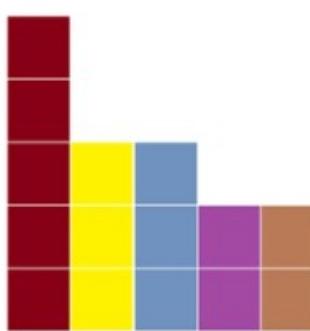
b



c



d



e

These bar charts are actually not very mathematically correct....does anyone know why?

I want to do a survey to gain information on lots of things. What would the difference be in the types of answers gained from these questions...

★ What kind of chart could you use to represent each one?

Height  
Hand span

Favourite film	Shoe size
Number of siblings	Next holiday destination

# Key terminology when describing data:

- Qualitative vs Quantitative

Qualitative data is non numerical and quantitative is numerical data.

- Continuous vs Discrete

Continuous data can take any value, it is measured whereas discrete data can only take certain values, there are a countable number of possible values.

- Categorical

When data is collected in to groups or categories.

- Raw

Raw data is collected from a source and nothing has been done to it.

<https://www.mathspad.co.uk/interactives/typesOfData/typesOfData.php>

# Statistics – The cycle

What do you want  
to find out?

Problem specification  
and analysis

Interpretation

Interpret the results.  
Has your question been  
answered?

## The Problem Solving Cycle

Information Collection

How are you going  
to gather data to  
help you find out?

Presenting and Representation

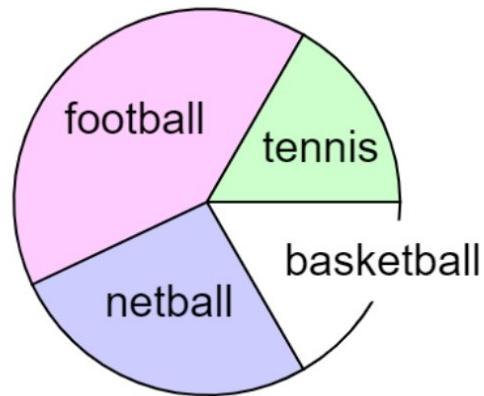
Represent the  
results.

Do some  
calculations to find

# This week: Discrete data

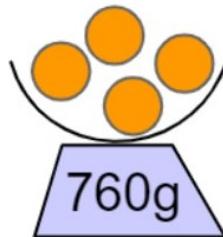
- Calculating and interpreting with discrete data (today!)
- Representing discrete data

The pie chart shows some people's favourite sports.  
What is the **mode**?



Mode = most common  
Football

Some oranges on a set of scales are shown.  
Work out the **mean**.



Mean: Add all the values together and divide by how many values there are

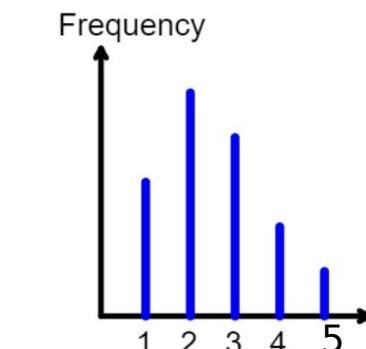
=

The salaries of some workers at a company are listed.  
Work out the **median**.

£16,000  
£16,000  
£24,000  
£27,000  
£31,000  
£106,000

Median: Put the values in order of size and find the middle  
Middle of £24,000 and £27,000:

A bar-line graph showing the number of children in some families.  
Work out the **range**.



Range = biggest value - smallest

Biggest number of children = 5  
Smallest number of children = 1

Answer the questions about the frequency table showing how many bars of chocolate people eat in a week...

<b>Bars</b>	<b>Frequency</b>	Total
0	7	0
1	2	2
2	8	16
3	2	6
4	6	24
5	1	5
6	0	0

Total people =  
26

Total bars =  
53

Mean number of bars =

Mean number of bars =

How many people ate 1 bar of chocolate? 2

How many people ate 3 or 4 bars of chocolate? 8

What is the largest number of bars eaten in 1 week? 5

What is the range of the number of bars?  $5 - 0 = 5$

What is the most common number of bars eaten? 2 bars (frequency of 8)

How many bars were eaten altogether? Total bars =

How many people were asked? 53

Total people =  
26

What is the mean number of bars eaten? 2

# Find the mean number of goals scored in 10 games...

Goals in a game	Frequency	Total
0	0	$0 \times 0 = 0$
1	2	$1 \times 2 = 2$
2	4	$2 \times 4 = 8$
3	1	$3 \times 1 = 3$
4	3	$4 \times 3 = 12$

*Total games*=10

*Total goals*=25

Think, to find the mean number of goals. What sum do we need to do?

$$\frac{\text{total goals}}{\text{total games}}$$

Total goals ~~25~~ 25

Total games ~~10~~ 10

$$\text{Mean } \frac{25}{10} = 2.5$$

On average, 2.5 goals are scored per game

### Worked Example

Calculate the mean number of siblings

Number of siblings	Frequency	total
0	2	0
1	3	3
2	1	2
3	2	6
4	2	8

$$\text{Total} = 10$$

$$\text{Total} = 19$$

- Find the total number of siblings:  
The sum of (number of siblings  $\times$  frequency)

$$\text{Total siblings} = 19$$

- Find the total number of people asked:

The sum of the frequency column

$$\begin{aligned}\text{Total asked} &= 10 \\ \text{Mean} &= 1.9\end{aligned}$$

### Your Turn

Calculate the mean number of siblings

Number of siblings	Frequency	total
0	4	0
1	6	6
2	2	4
3	4	12
4	4	16

$$\text{Total} = 20$$

$$\text{Total} = 38$$

$$\text{Total siblings} = 38$$

$$\begin{aligned}\text{Total asked} &= 20 \\ \text{Mean} &= \end{aligned}$$

1. Find the mean number of siblings:

<b>Siblings</b>	<b>Frequency</b>
0	10
1	7
2	6
3	2
4	5

You have a  
go...

Total siblings =

Total people asked =

Mean =

2. Find the mean number pies eaten per month:

<b>Pies eaten in 1 month</b>	<b>Frequency</b>
0	10
1	5
2	2
3	1
4	10

Total pies =

Total people asked =

Mean =

3. Find the averages and range for this table showing the number of goals scored in hockey matches:

<b>Goals per game</b>	<b>Frequency</b>
0	11
1	5
2	1
3	1
4	2

Mean =

1. Find the mean number of siblings:

Siblings	Frequency
0	10
1	7
2	6
3	2
4	5

## ANSWERS

Total siblings = 45

Total people asked 30

Mean = 1.5

2. Find the mean number pies eaten per month:

Pies eaten in 1 month	Frequency
0	10
1	5
2	2
3	1
4	10

Total pies = 52

Total people asked 28

=

Mean = 1.8  
6(3 sf)

3. Find the mean for this table showing the number of goals scored in hockey matches:

Goals per game	Frequency
0	11
1	5
2	1
3	1
4	2

Mean = 0.9

# Finding the mode, median and range



What is special about the range??

Together

6<sup>th</sup> person lies in this group

Number of siblings	Frequency
0	2
1	4
2	1
3	2
4	2

Mode = most common number of siblings (with the highest frequency) **sibling**

Range = biggest number of siblings - smallest number of siblings **Range = 4 - 0 = 4**

Median = how many siblings the middle person has.  
Middle person = **Median = 1 sibling**

Your turn

11<sup>th</sup> person lies in this group

Number of siblings	Frequency
0	4
1	7
2	2
3	4
4	4

Mode = most common number of siblings (with the highest frequency) **sibling**

Range = biggest number of siblings - smallest number of siblings **Range = 4 - 0 = 4**

Median = how many siblings the middle person has.  
Middle person = **Median = 1 sibling**

1. Find the mode, median and range

Siblings	Frequency
0	10
1	7
2	6
3	2
4	5

You have a go...

Mode =

Range =

Median =

2. Find the mode, median and range

Pies eaten in 1 month	Frequency
0	10
1	5
2	2
3	1
4	10

Mode =

Range =

Median =

3. Find the averages and range for this table showing the number of goals scored in hockey matches:

Goals per game	Frequency
0	11
1	5
2	1
3	1
4	2

Mode =

Range =

Median =

1. Find the mode, median and range

Sibling s	Freque ncy
0	10
1	7
2	6
3	2
4	5

## ANSWERS

Mode = 0 siblings

Range =  $4 - 0 = 4$

Median = 1 sibling  
30 people altogether.  
15.5<sup>th</sup> person has 1 sibling

3. Find the averages and range for this table showing the number of goals scored in hockey matches:

Goals per game	Freque ncy
0	11
1	5
2	1
3	1
4	2

2. Find the mode, median and range

Pies eaten in 1 month	Freque ncy
0	10
1	5
2	2
3	1
4	10

Mode = 0 and 4 pies

Range =  $4 - 0 = 4$

Median = 1 pie  
28 people altogether.  
 $14.5^{th}$  = 1 pie

# Challenge!

Class A scores: 9 6 6 6 10 2 10 3

Class B scores: 3 9 3 6 10 3 9 10

Make 2 comparisons about the classes.

Who do you think is the best class? Why?

Why might some people disagree with your answer?

**Class A**

Mode = 6

Median = 6

Mean = 6.5

Range = 8

**Class B**

Mode = 3

Median = 7.5

Mean = 6.625

Range = 7

Which average was perhaps  
not the best to use??

# Extension

- Solving simultaneous equations needed to answer the following questions...



The table shows the number of days that 30 pupils were absent in a term.

Days absent, $x$	0	1	2	3	4	5
Frequency, $f$	14	$a$	3	$b$	1	2

Given that the mean number of days absent was 1.4, work out the values of  $a$  and  $b$ .

Hint: Can you form 2 equations from the information given?

$$14 + a + 3 + b + 1 + 2 = 30$$

$$\frac{0 + a + 6 + 3b + 4 + 10}{30} = 1.4$$

$$20 + a + b = 30$$

$$0 + a + 6 + 3b + 4 + 10 = 42$$

$$a + b = 10$$

$$a + 3b + 20 = 42$$

$$a + 3b = 22$$

$$a + b = 10$$

$$a + 3b = 22$$

$$2b = 12$$

$$b = 6$$

$$a = 4$$



The table shows the number of days that 30 pupils were absent in a term.

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Hint: Can you form 2 equations from the information given?

$$14 + a + 3 + b + 1 + 2 = 30$$

$$\frac{0 + a + 6 + 3b + 4 + 10}{30} = 1.4$$

$$a + b = 10$$

$$20 + a + b = 30$$

$$0 + a + 6 + 3b + 4 + 10 = 42$$

$$a + 3b = 22$$

$$a + b = 10$$

$$a + 3b + 20 = 42$$

$$2b = 12$$

$$a + 3b = 22$$

$$b = 6$$

$$a = 4$$

2. This table shows how many mobile phones are confiscated from classes:

Mobiles Confiscated	Number of classes
0	11
1	$a$
2	3
3	1

The mean number of mobiles confiscated from a class is 0.7. What is the missing value in the table?

1. This table shows how many calls 100 people receive in a day. Given that the mean number of calls is 2.41. Find the values of  $a$  and  $b$ .

Calls	0	1	2	3	4	5
Frequency	20			12		18

1. This table shows how many calls 100 people receive in a day. Given that the mean number of calls is 2.41. Find the values of  $a$  and  $b$

Calls	0	1	2	3	4	5
Frequency	20			12		18

$$20 + a + 20 + 12 + b + 18 = 100$$

$$70 + a + b = 100$$

$$a + b = 30$$

$$\frac{0 + a + 40 + 36 + 4b + 90}{100} = 2.41$$

$$0 + a + 40 + 36 + 4b + 90 = 241$$

$$166 + a + 4b = 241$$

$$a + 4b = 75$$

$$a + b = 30$$

$$a + 4b = 75$$

$$3b = 45$$

$$b = 15$$

$$a = 15$$

2. This table shows how many mobile phones are confiscated from classes:

Mobiles Confiscated	Number of classes
0	11
1	a
2	3
3	1

The mean number of mobiles confiscated from a class is 0.7. What is the missing value in the table?

$$\begin{aligned}11 + a + 3 + 1 &= n \\15 &= n - a \\15 &= 0.3n + 9 \\ \frac{0 + a + 6 + 3}{n} &= 0.7 \\15 &= 0.3n + 9 \\6 &= 0.3n \\9 + a &= 0.7n \\n &= 20 \\a &= 0.7n - 9 \\a &= 5\end{aligned}$$